SECTION 2.1: PREVIEW OF CALCULUIS

goals: To understand

- the difference between a secant line and a tangent line.
- how to use secant lines to estimate the slope of a tangent line.
- how to use average velocity to estimate instantaneous velocity.
- why our present tools force us to *estimate* slope or instantaneous velocity and not calculate it explicitly.

1. REVIEW: Write the equation of the line through the points $P(-3, 1)$ and $Q(2, 4)$.

2. The point $P(2, 3)$ lies on the graph of $f(x) = x + \frac{2}{x}$. For each value of x in the table below, find the slope of the secant line between $P(2, 3)$ and $Q(x, f(x))$, *if possible*.

point Q		slope of secant line PQ
x-value	y-value	PQ
$x = 4$		
$x = 3$		
$x = 2.5$		
$x = 2.25$		
$x = 2.1$		
$x = 2$		
$x = 1.9$		
$x = 1.75$		
$x = 1.5$		
$x = 1$		

(a) Now, use technology to sketch a rough graph $f(x)$ on the interval $(0, 5]$ and add the secant lines from part a. (Your graph may be messy...It's ok.) Add in the tangent line to the graph at P. Label the secant lines with their respective slopes. What can you conclude about the slope of the tangent line to $f(x)$ at P?

(b) Write a best guess for the equation of the line tangent to $f(x)$ at point P. Is your equation plausible?

3. The table shows the position of a cyclist after accelerating from rest.

t (hours)	0	0.5	1	1.5	2	2.5	3	3.5	4
d (miles)	0	6.2	13.4	23.1	33.4	44.6	54.7	62.6	70

(a) What is the cyclist's average velocity on the 4 hours of the bike ride?

(b) Estimate the cyclist's average velocity in miles per hour on each of the time intervals below:

i. $[0, 1.5]$

ii. $[0.5, 1.5]$

iii. $[1, 1.5]$

iv. $[1.5, 2]$

v. $[1.5, 2.5]$

vi. $[1.5, 3]$

(c) The calculations above can be used to estimate the *instantaneous* velocity of the cyclist at what time? What would your estimate be?

BONUS: If you understood what we did in class today, you should be able to answer the questions below.

4. In words, what is a secant line, what is a tangent line and how are they different?

5. Justify the assertion that the problem of finding the slope of the tangent to a graph at a point is the same problem as finding the instantaneous velocity of an object given its position.

6. Explain why the method we use to find the slope of the secant line (i.e. $m_{sec} = \frac{y_2 - y_1}{x_2 - x_1}$) *cannot* be used to find the slope of the tangent line?