

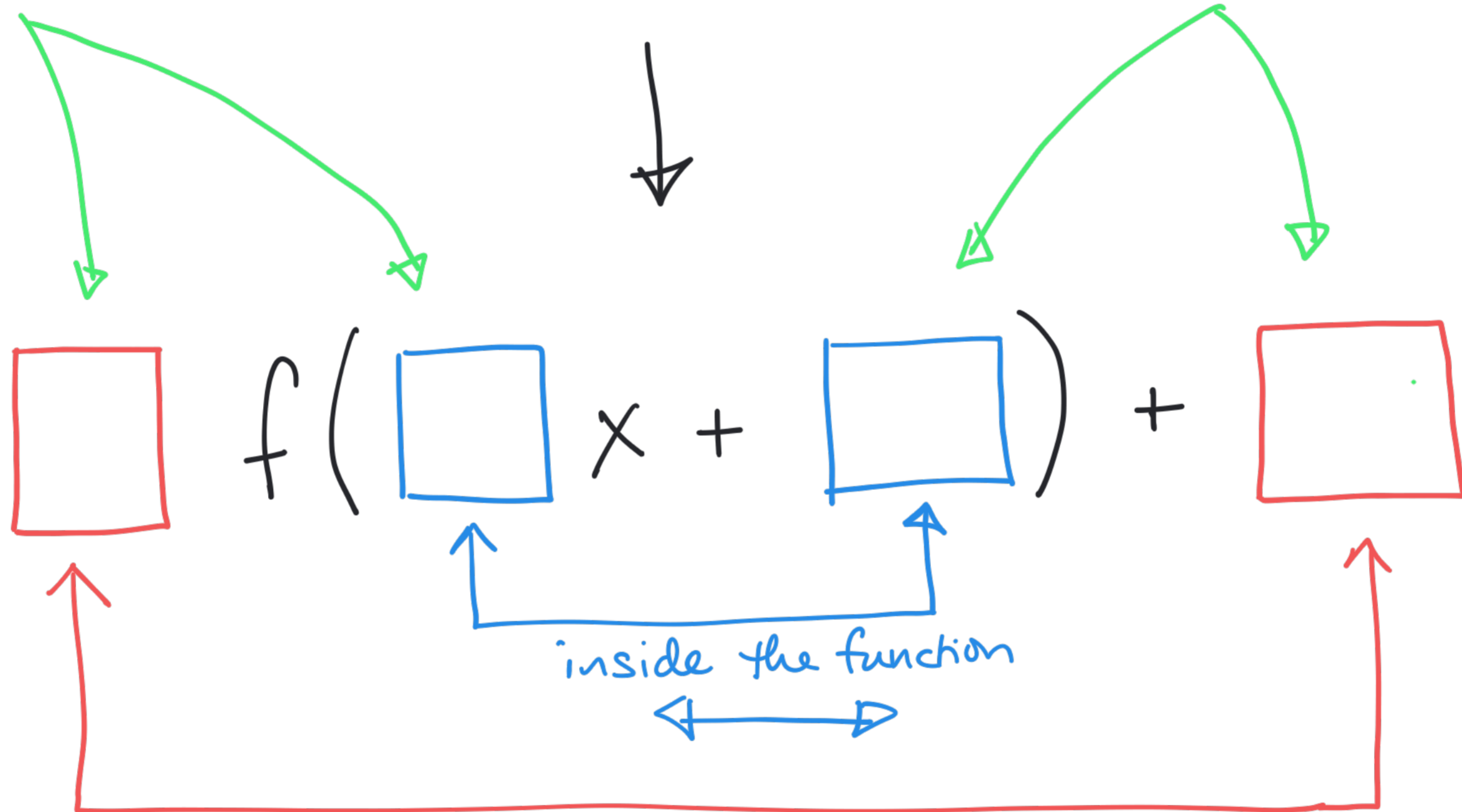
Intro video: Section 1.3  
Transformations of Functions

Math F251X Fall 2020

SCALING  
do these first

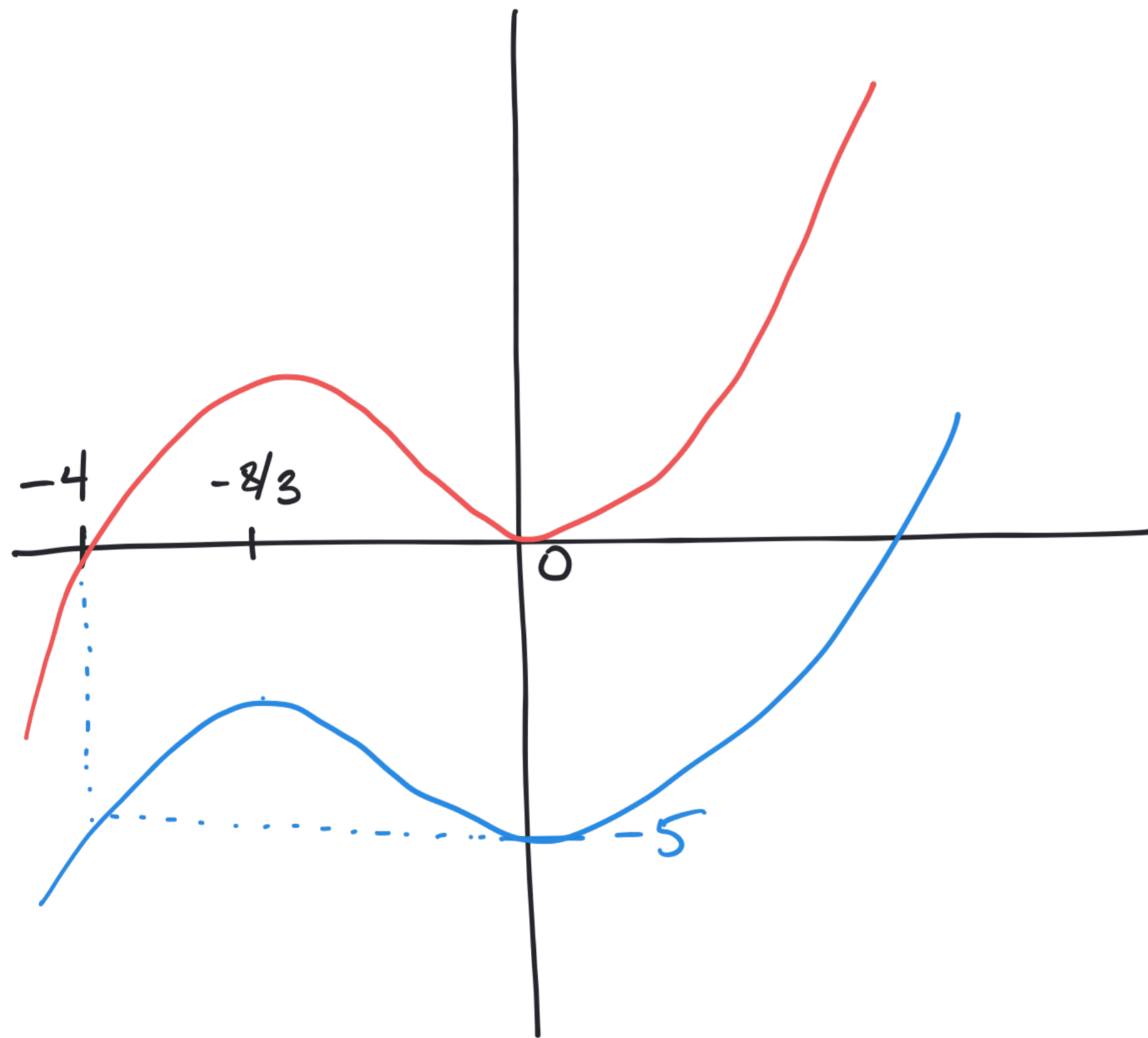
$$f(x)$$

SHIFTING  
do these next



outside the function  
move the graph

$$f(x) \rightarrow f(x) + c$$

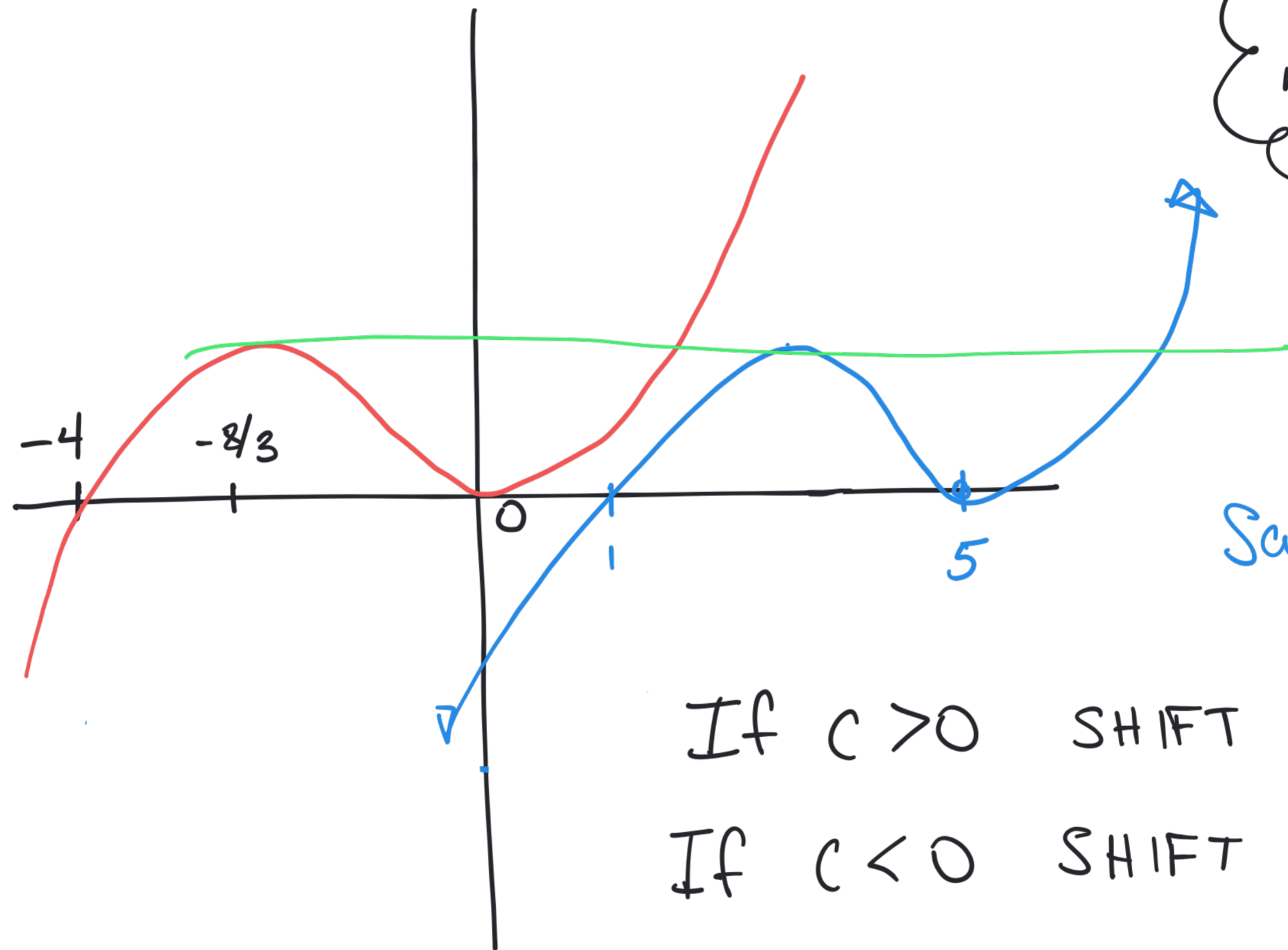


Shift  $\uparrow$   
if  $c > 0$

Shift  $\downarrow$   
if  $c < 0$

$$c = -5$$

$$f(x) \rightarrow f(x - c)$$

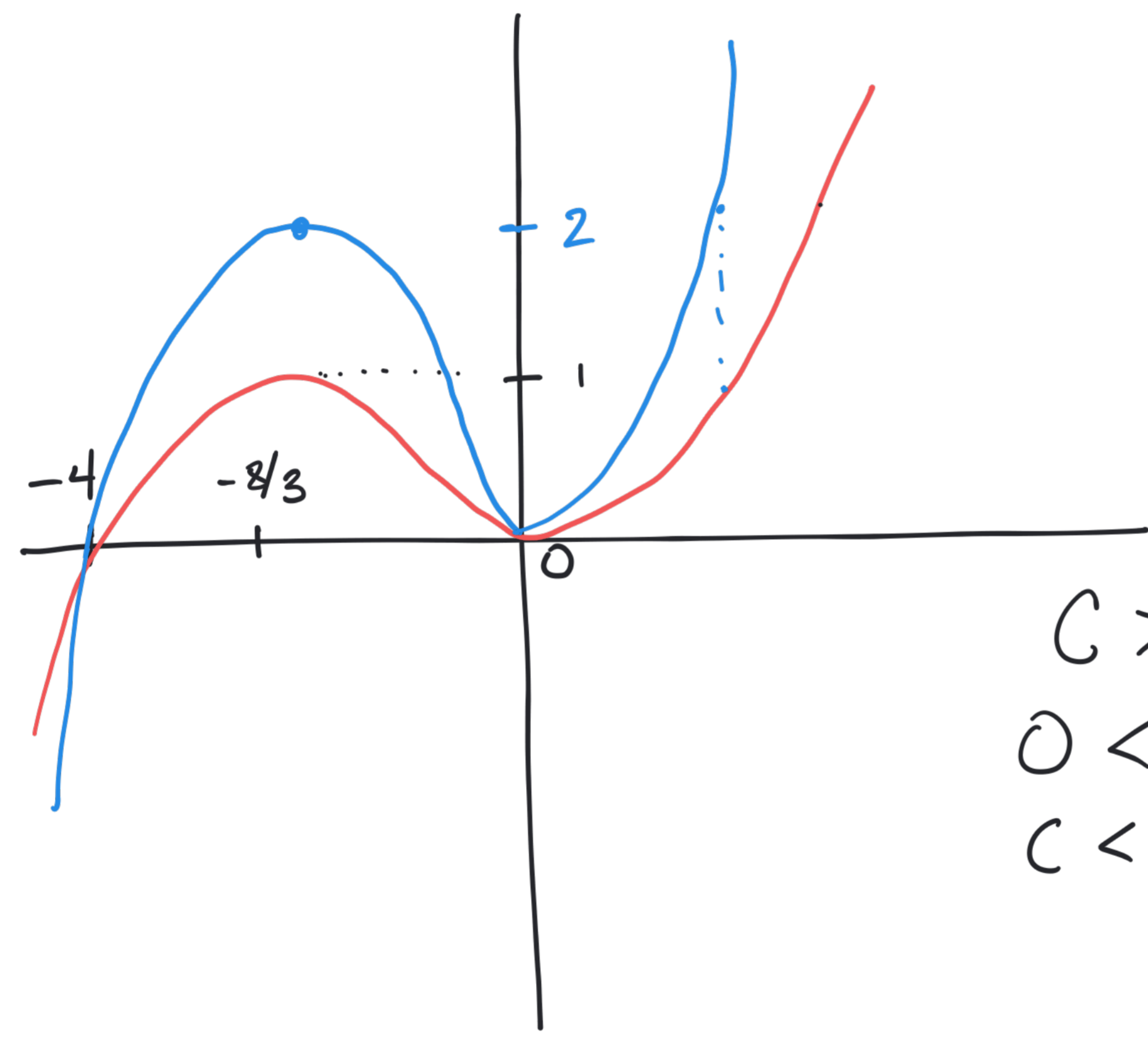


old behavior  
at 0 is  
new behavior  
at c




Say  $c = -5$

If  $c > 0$  SHIFT ←  
If  $c < 0$  SHIFT →

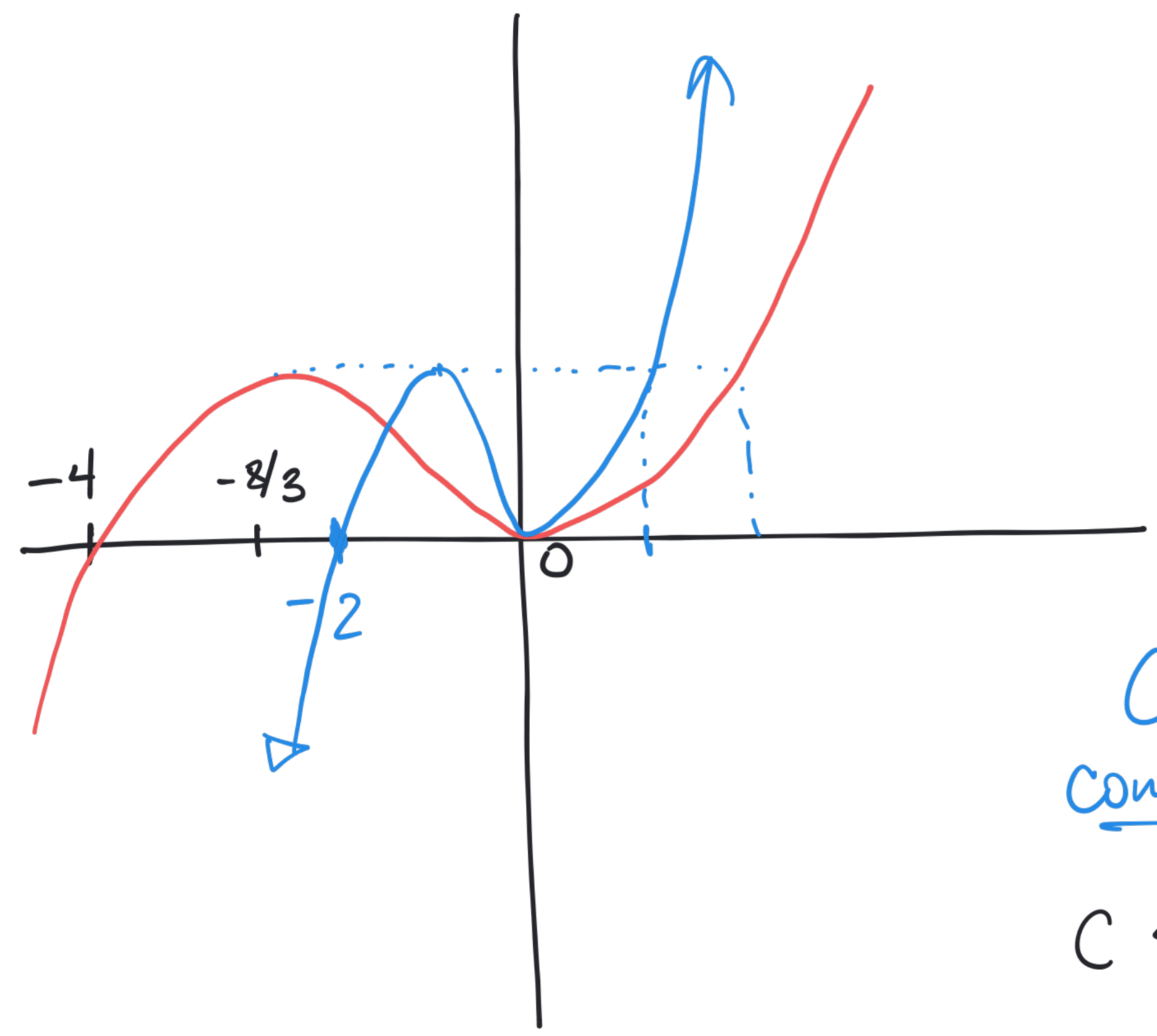
$$f(x) \rightarrow cf(x)$$



$$c = 2$$

- $c > 1$  : stretch 
- $0 < c < 1$  : compress 
- $c < 0$  : flip over x-axis and then stretch 

$$f(x) \rightarrow f(cx)$$



Old behavior  
at 1 is new  
behavior at  
 $1/c$

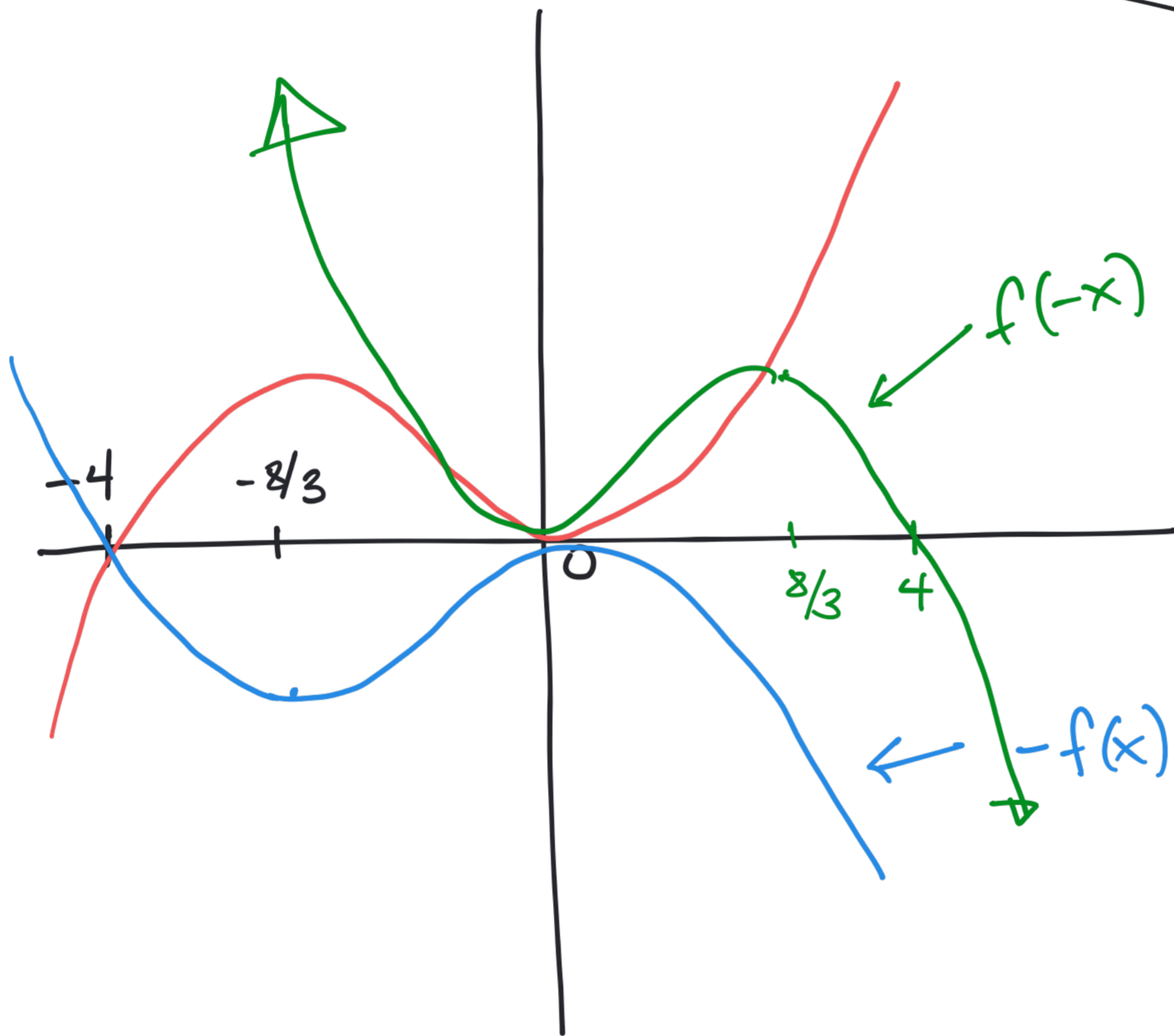
$C = 2$   
Compress by 2  $\longleftrightarrow$

$C < 0$  : flip across  
y-axis as  
well

$f(x)$

$-f(x)$

$f(-x)$



$-f(x)$ : flips  $\updownarrow$   
(over x-axis)

$f(-x)$ : flips  $\leftrightarrow$

$$f(x) \rightarrow -f(\underline{2x}) + 3$$

