

Name: \_\_\_\_\_ / 12

- There are 12 points possible on this proficiency: one point per problem with no partial credit.
- You have **30** minutes to complete this proficiency.
- No aids (book, calculator, etc.) are permitted.
- Do **not** simplify your expressions.
- **Your final answers should start with**  $f'(x) =$ ,  $\frac{dy}{dx} =$  or something similar.
- Box your final answer.

*Note that this sample derivative proficiency is slightly different from the actual derivative proficiency, because there are a few functions ( $\ln(x)$ , inverse trig functions, implicit differentiation in general) that we haven't covered yet.*

1. [12 points] Compute the derivatives of the following functions.

a.  $f(x) = \sqrt[5]{x} + 4x^3 + \frac{x - \sqrt{2}}{9}$

b.  $y = x^3 \tan(x)$

c.  $y = \frac{\sec(x)}{1 + e^x}$

d.  $y = \sin(ax)e^{bx^2}$  where  $a$  and  $b$  are fixed constants.

e.  $f(x) = \frac{\cos(x)}{\sin(x)}$

f.  $g(x) = \sqrt{2 + \sin^2(6x)}$

g.  $y = \tan(x^3 \cdot 5^x)$

h.  $f(z) = \sec(\sqrt{z})$

i.  $y = \sin\left(\frac{x}{x-3}\right)$

j.  $h(x) = \cos(e^{\pi x} - (4x)^9)$

k.  $g(x) = (\sin(x^2 + x))^5$

l.  $f(x) = \frac{1}{9x}$