

1. The graph of a function f is shown below. Find the following:

a) $f(1)$ and $f(5)$

$$f(1) = 3, f(5) \approx -0.6$$

b) the domain of f

$$[0, 7]$$

c) the range of f

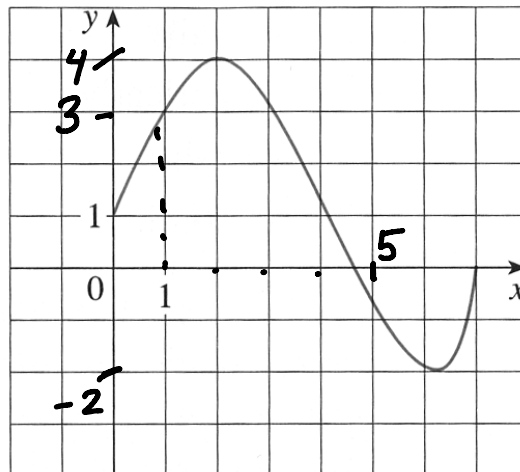
$$[2, 4]$$

d) For which value of x is $f(x) = 4$?

$$x = 2$$

e) Where is f increasing?

$$\text{when } x \text{ is in } (0, 2) \cup (6.1, 7)$$



2. Let $f(x) = 3x^2 - x + 2$. Find and simplify the following expressions. Are (b) and (c) different?

(a) $f(2) = 3(2)^2 - 2 + 2 = 12$

(b) $f(a^2) = 3(a^2)^2 - a^2 + 2 = 3a^4 - a^2 + 2$

(c) $[f(a)]^2 = [3a^2 - a + 2]^2 = 9a^4 - 3a^3 + 6a^2 - 3a + a^2 - 2a + 6a^2 - 2a + 4$
 $= 9a^4 - 6a^3 + 13a^2 - 4a + 4$

(d) $\frac{f(a+h) - f(a)}{h} = \frac{3(a+h)^2 - (a+h) + 2 - [3a^2 - a + 2]}{h}$

$$= \frac{3a^2 + 6ah + 3h^2 - a - h + 2 - 3a^2 + a - 2}{h} = \frac{6ah + 3h^2 - h}{h}$$

$$= 6a + 3h - 1$$

3. Write a formula for the top half of the circle with center (2, 0) and radius 3.

Circle: $(x-2)^2 + y^2 = 9$

top half: $y = \sqrt{9 - (x-2)^2}$

4. Find the domain of each of the following functions. Use interval notation.

(a) $f(x) = \frac{1}{x^2 - 16}$

want to avoid:

$x^2 - 16 = 0$

$(x-4)(x+4) = 0$

$x = \pm 4$

answer: $(-\infty, -4) \cup (-4, 4) \cup (4, \infty)$

or

all real numbers except $x = 4$ or $x = -4$

(b) $f(x) = \sqrt{x} + \sqrt{11-x}$

want $x \geq 0$ and $11-x \geq 0$

or $x \geq 0$ and $11 \geq x$

answer: $[0, 11]$

(c) $g(x) = \ln(x-4)$

want $x-4 > 0$

so $x > 4$

answer: $(-\infty, 4)$

(d) $h(x) = e^{-x} = \frac{1}{e^x}$

but $e^x \neq 0$.

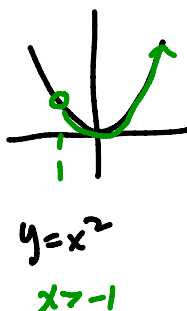
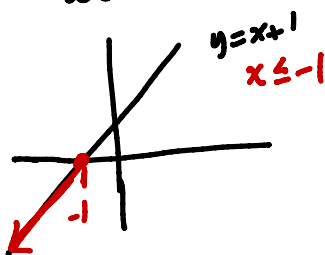
So all x 's are fine!

answer: $(-\infty, \infty)$

5. Graph the piecewise defined function.

$$f(x) = \begin{cases} x+1 & \text{if } x \leq -1 \\ x^2 & \text{if } x > -1 \end{cases}$$

work



answer

