LECTURE NOTES: §1.4 & 1.5

1. On the same set of axes, graph $f(x) = 2^x$, $g(x) = e^x$, $h(x) = 10^x$, and $k(x) = \left(\frac{1}{2}\right)^x$.

2. Assume a > 0. What is the domain and range of $f(x) = a^x$? Asymptotes?

3. Without the use of a calculator, compute the following:

- (a) $\log_2 \frac{1}{16} =$
- (b) $\ln e^{0.24} =$
- (c) $e^{5\ln x} =$
- 4. On the same set of axes, graph $f(x) = e^x$ and $g(x) = \ln x$.

5. Solve the following equations for *x*.

(a)
$$\ln(x+5) - 1 = 7$$
 (b) $e^{2x-5} + 4 = 10$

- 6. Are the following statements true or false? If either case, explain why. If possible, change the false statements so that they are a true statement.
 - (a) $(a+b)^2 = a^2 + b^2$ (b) $\sqrt{x^2+4} = x+2$ (c) $\frac{a+b}{c+d} = \frac{a}{c} + \frac{b}{d}$
 - (d) $\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$
 - (e) $\ln(x+y) = \ln x + \ln y$
 - (f) $\frac{\ln x}{\ln y} = \ln\left(\frac{x}{y}\right)$
 - (g) $\ln(x-y) = \ln\left(\frac{x}{y}\right)$
 - (h) $f^{-1}(x) = \frac{1}{f(x)}$ (i) $f^{2}(x) = (f(x))^{2}$

UAF Calculus 1