

5. Find the derivatives of the functions below using the rules discussed in class today. (Chain rule, quotient rule, product rule not needed!)

(a) $f(x) = 6.1x^3 + \pi x + e^2 + 4e^x$

$$f'(x) = 18.3x^2 + \pi + 4e^x$$

(b) $f(x) = \frac{8}{x^4} - \frac{x^2}{7} + \frac{\sqrt{5}}{2} = 8x^{-4} - \frac{1}{2}x^2 + \frac{\sqrt{5}}{2}$

$$f'(x) = -32x^{-5} - x$$

(c) $y = 6x^{5/3} - x^{1/3}$

$$y' = \frac{30}{3} x^{2/3} - \frac{1}{3} x^{-2/3}$$

(d) $y = \frac{x^2 + 5\sqrt{x} + 1}{\sqrt{x}} = x^{3/2} + 5 + x^{-1/2}$

$$y' = \frac{3}{2} x^{1/2} + 0 + \left(-\frac{1}{2}\right) x^{-3/2} = \frac{3}{2} \sqrt{x} - \frac{1}{2} x^{-3/2}$$

(e) $y = x(x+1) = x^2 + x$

$$y' = 2x + 1$$

(f) $y = ax^2 + \frac{b}{x} + c = ax^2 + bx^{-1} + c$ and a, b, c fixed constants

$$\boxed{\frac{dy}{dx}} = 2ax - bx^{-2}$$