

Name: \_\_\_\_\_

- There are 12 points possible on this proficiency, one point per problem. **No partial credit will be given.**
- You have 1 hour to complete this proficiency.
- No aids (book, calculator, etc.) are permitted.
- You do **not** need to simplify your expressions.
- Correct parenthesization is required.
- Your final answers **must start with**  $f'(x) =$ ,  $dy/dx =$ , or similar.
- **Circle or box your final answer.**

1. [12 points] Compute the derivatives of the following functions.

a.  $f(x) = \frac{2x}{3} + \frac{2}{3x} - \frac{2\pi}{3}$

b.  $G(\theta) = \theta^2 \tan(\theta)$

c.  $h(x) = \sqrt{x^4 - 16}$

**d.**  $y = \cot(x)$

**e.**  $k(x) = \arcsin(4x)$

**f.**  $R(\theta) = \left(2\theta + \cos\left(\frac{\theta}{\pi}\right)\right)^5$

g.  $y = (7x - 1)^{-2/3} \ln(x)$

h.  $y = \ln(5) + e^{5x} + \sec(2x)$

i.  $f(x) = (b^2 + \ln(bx^2 + 1))^{7.8}$  (Assume  $b$  is a fixed constant.)

j.  $y = \frac{5e^x}{x - e^x}$

k.  $f(x) = x \left( \frac{2x - x^{-2}}{3x^2} \right)$

l. Find  $\frac{dy}{dx}$  for  $\sin(y^2) = x + y + \sqrt{2}$ .