

Name: _____

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- There are 12 points possible on this proficiency, one point per problem. **No partial credit will be given.**
- You have one hour to complete this proficiency.
- No aids (book, calculator, etc.) are permitted.
- You do **not** need to simplify your expressions.
- Your final answers **must start with** $f'(x) =$, $\frac{dy}{dx} =$, or similar.
- Draw a box around your final answer.

1. $u(x) = (e^2 + e^x)(7 - x^{-5})$

$$u'(x) = (e^2 + e^x)(-(-5)x^{-6}) + (7 - x^{-5})(e^x)$$

$$= 5x^{-6}(e^2 + e^x) + (7 - x^{-5})e^x$$

alternately

$$u(x) = 7e^2 + 7e^x - e^2 \cdot x^{-5} - e^x x^{-5}$$

$$u'(x) = 0 + 7e^x - e^2(-5x^{-6}) - (e^x(-5x^{-6}) + x^{-5}(e^x))$$

2. $f(t) = \frac{1}{\sqrt[3]{t}} + \left(\frac{2 + \pi t}{3}\right)^4 = t^{-1/3} + \left(\frac{2}{3} + \frac{\pi}{3}t\right)^4$

$$f'(t) = -\frac{1}{3}t^{-4/3} + 4\left(\frac{2}{3} + \frac{\pi}{3}t\right)^3 \left(\frac{\pi}{3}\right)$$

3. $g(y) = \frac{\tan(y^2)}{1 + \sin(y)}$

$$g'(y) = \frac{(1 + \sin(y))(\sec^2(y^2))(2y) - \tan(y^2)(\cos(y))}{(1 + \sin(y))^2}$$

4. $y = (2x^2 + 4) \arctan(x)$ (note $\arctan(x) = \tan^{-1}(x)$)

$$y' = (2x^2 + 4) \left(\frac{1}{1+x^2} \right) + \arctan(x) (4x)$$

5. $h(x) = \frac{x^5 - ax + b}{x^2}$ (where a and b are constants)

$$= x^3 - ax^{-1} + bx^{-2}$$

$$h'(x) = 3x^2 - a(-x^{-2}) + b(-2x^{-3})$$

$$= 3x^2 + \frac{a}{x^2} - \frac{2b}{x^3}$$

or, $h'(x) = \frac{x^2(5x^4 - a) - (x^5 - ax + b)(2x)}{x^4}$ but don't do this.

6. $G(x) = e^{\cos(x^2)+2}$

$$G'(x) = e^{\cos(x^2)+2} (-\sin(x^2))(2x)$$

$$7. g(u) = \ln(2) + \ln(u) - \ln(u^2) \quad \leftarrow = \ln(2) + \ln(u) - 2\ln(u)$$

$$g'(u) = \frac{1}{u} - \frac{1}{u^2} (2u)$$

$$g'(u) = \frac{1}{u} - \frac{2}{u} = -\frac{1}{u}$$

$$8. f(\theta) = 2\sin(\theta^3 + 2)$$

$$f'(\theta) = 2\cos(\theta^3 + 2)(3\theta^2)$$

$$9. k(x) = e^{3x}\cos(2x)$$

$$k'(x) = e^{3x}(-\sin(2x)(2)) + \cos(2x)(e^{3x})(3)$$

10. $F(x) = \csc(x) + (\sqrt{2})x$

$$F'(x) = -\csc(x) \cot(x) + \sqrt{2}$$

11. $g(t) = \frac{6}{\cos(t)} = 6 \sec(t)$

$$g'(t) = 6 \sec(t) \tan(t)$$

or
$$g(t) = 6 (\cos(t))^{-1}$$
$$g'(t) = -6 \cos(t)^{-2} (-\sin t)$$
$$= \frac{6 \sin t}{\cos^2 t}$$

or
$$g'(t) = \frac{\cos(t)(0) - 6(-\sin(t))}{(\cos(t))^2}$$
$$= \frac{6 \sin t}{\cos^2 t}$$

12. Compute $\frac{dy}{dx}$ if $xy - 2y = 2 + e^y$. You **must** solve for $\frac{dy}{dx}$.

$$x \frac{dy}{dx} + y - 2 \frac{dy}{dx} = e^y \frac{dy}{dx}$$

$$\frac{dy}{dx} (x - 2 - e^y) = -y$$

$$\frac{dy}{dx} = \frac{-y}{x - 2 - e^y}$$