

Name: _____

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Instructor: Bueler | Jurkowski | Maxwell

There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [15 points] Compute the derivatives of the following functions. You need not simplify your answers.

a. $f(x) = x^{\frac{3}{2}} + 9 - e^x$

$$f'(x) = \frac{3}{2}x^{1/2} - e^x$$

b. $g(w) = 7w - \frac{\pi}{w^2}$

$$g'(w) = 7 - \pi \frac{d}{dw} w^{-2} = 7 + 2\pi w^{-3} = 7 + \frac{2\pi}{w^3}$$

c. $h(x) = \frac{1}{4-x^2}$

$$h'(x) = -\frac{\frac{d}{dx}(4-x^2)}{(4-x^2)^2} = \frac{2x}{(4-x^2)^2}$$

d. $R(s) = (s^2 - 1)e^s$

$$R'(s) = 2se^s + (s^2 - 1)e^s = (s^2 + 2s - 1)e^s$$

e. $f(x) = \frac{3-x^3}{2+x}$

$$f'(x) = \frac{\left[\frac{d}{dx}(3-x^3) \right] (2+x) - (3-x^3) \frac{d}{dx}(2+x)}{(2+x)^2} = \frac{-3x^2(2+x) - (3-x^3)}{(2+x)^2} = -\frac{3+6x^2+2x^3}{(2+x)^2}$$

2. [4 points] Find the equation of the tangent line to the graph of $y = \sqrt{3x}$ at $x = 2$.

$$\frac{dy}{dx} = \frac{d}{dx} \sqrt{3} x^{1/2} = \frac{\sqrt{3}}{2} x^{-1/2}$$

$$\text{@ } x=2: y = \sqrt{6}$$

$$\frac{dy}{dx} = \frac{\sqrt{3}}{2\sqrt{2}}$$

$$\text{tangent line } y = \sqrt{6} + \frac{\sqrt{3}}{2\sqrt{2}} (x - 2)$$

3. [6 points] The temperature in $^{\circ}\text{C}$ of coffee in a cup is given by

$$T(t) = 20 + \frac{50}{e^t}$$

where t is measured in hours.

- a. What is the temperature of the coffee at time $t = 0$? Include units in your answer.

$$T(0) = 20 + \frac{50}{1} = 70^{\circ}\text{C}$$

- b. What is the rate of change of temperature of the coffee at time $t = 0$? Include units in your answer.

$$T'(t) = \frac{d}{dt} \frac{50}{e^t} = -\frac{50}{(e^t)^2} e^t = -50e^{-t}$$

$$T'(0) = -50e^{-0} = -50^{\circ}\text{C}/\text{hour}$$