

Name: \_\_\_\_\_ / 25

There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [15 points] Find the derivatives of each of the following. You do not need to simplify your answer.

a.  $h(\theta) = e^2 \sec(\theta) + \csc(\theta)$

b.  $y = \sin(5x^2)$

c.  $f(x) = \frac{\tan(x)}{x + 4 \cos(x)}$

d.  $f(q) = q^3 e^{6q+5}$

e.  $k(t) = (\sqrt[4]{t} - 7t + 3)^4$

2. [4 points] Find an  $x$ -value such that the function  $f(x) = 2x - \sin(4x)$  has a horizontal tangent line. (You do not have to find *every* value. Simply find one.)

3. [6 points] In a certain experiment involving bacteria, the number  $N$  of bacteria in a culture after  $t$  days is modeled by the function

$$N(t) = 800 \left( 1 + \frac{3}{(t^2 + 1)^2} \right).$$

- a. How many bacteria are in the culture at the beginning of the experiment?
- b. Compute  $N'(t)$ . (You do not need to simplify, but you may if you choose.)
- c. After one day, is the number of bacteria in the culture **increasing** or **decreasing**, and how do you know? (Justify your answer; an answer with no justification will receive no credit.)