Name: $\qquad$
There are 20 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [8 points] Use the graph of the function of $f(x)$ to answer the following questions. If a value does not exist, write DNE.

a. $f(-3)=$
b. $f(1)=$ $\qquad$
c. $\lim _{x \rightarrow-3^{-}} f(x)=$ $\qquad$
d. $\lim _{x \rightarrow-3^{+}} f(x)=$ $\qquad$
e. $\lim _{x \rightarrow-3} f(x)=$ $\qquad$
f. $\lim _{x \rightarrow 1} f(x)=$ $\qquad$
g. $\lim _{x \rightarrow-6} f(x)=$ $\qquad$
h. $\lim _{x \rightarrow 5^{+}} f(x)=$ $\qquad$
2. [2 points] The table below shows total active COVID cases in the Fairbanks North Star Borough over the time period between 7/13/2020 and 8/31/2020 (number of active cases measured on Mondays).

| date | $7 / 13$ | $7 / 20$ | $7 / 27$ | $8 / 3$ | $8 / 10$ | $8 / 17$ | $8 / 24$ | $8 / 31$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $t$ (week) | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| $C$ (\# of cases) | 146 | 167 | 192 | 215 | 238 | 275 | 332 | 409 |

a. What was the average rate of change in the number of cases over the 7 weeks? Show your work and include correct units in your answer.
b. What was the average rate of change in the number of cases from week 2 to week 5 ? Show your work and include correct units in your answer.
3. [6 points] Compute the following infinite limits. For each limit, justify your answer with a sentence or two, perhaps with a rough sketch. An answer with no justification will not receive full credit.
a. $\lim _{x \rightarrow 7^{-}} \frac{x^{2}-6}{x-7}=\square$
b. $\lim _{x \rightarrow 3^{+}} 18 \ln (x-3)=\square$
4. [4 points] On the axes below, sketch the graph of the function

$$
f(x)= \begin{cases}1-x^{2} & x<0 \\ 4 & x=0 \\ 3-x & x>0\end{cases}
$$

Then compute, with brief justification, the requested values in the table. An answer with no justification will not receive full credit.


| Value | Justification |
| :---: | :---: |
| $f(0)=$ |  |
| $\lim _{x \rightarrow 0^{-}} f(x)=$ |  |
|  |  |
| $\lim _{x \rightarrow 0} f(x)=$ |  |

