

Name: Solutions

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There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. **Show all work for full credit.**

1. [15 points] Find the derivative of each function below. You do not need to simplify your answer.

a. $F(x) = \sqrt{1+x^4} = (1+x^4)^{1/2}$

$$F'(x) = \frac{1}{2} (1+x^4)^{-1/2} (4x^3) = \frac{2x^3}{\sqrt{1+x^4}}$$

b. $f(x) = 3 \csc(x)$

$$f'(x) = -3 \csc(x) \cot(x)$$

c. $G(x) = \frac{1}{\sin^2(x) + \cos^2(x)} = \frac{1}{1} = 1$

$$G'(x) = 0$$

d. $g(\theta) = \tan(\theta^2 + 1)$

$$g'(\theta) = \sec^2(\theta^2+1) (2\theta) = 2\theta \sec^2(\theta^2+1)$$

e. $h(x) = \sec(x) + (\cot(x))^2$

$$\begin{aligned} h'(x) &= \sec(x) \tan(x) + 2(\cot(x))' (-\csc^2(x)) \\ &= \sec(x) \tan(x) - 2 \cot(x) \csc^2(x) \end{aligned}$$

2. [6 points] Find $\frac{d^3y}{dx^3}$ for $y = x^2 + 5 \sin(x)$.

$$y = x^2 + 5 \sin(x)$$

$$\frac{dy}{dx} = 2x + 5 \cos(x)$$

$$\frac{d^2y}{dx^2} = 2 - 5 \sin(x)$$

$$\frac{d^3y}{dx^3} = -5 \cos(x)$$

3. [4 points] Determine where the graph of $f(x) = \frac{4}{x^2+2x}$ has a horizontal tangent.

$$f(x) = 4(x^2+2x)^{-1}; \text{ horizontal tangent means } f' = 0.$$

$$f'(x) = 4(-1)(x^2+2x)^{-2}(2x+2)$$

$$= \frac{-4(2x+2)}{(x^2+2x)^2} = \frac{-8(x+1)}{(x^2+2x)^2} = 0$$

$$\text{So } -8(x+1) = 0.$$

$$\text{So } \boxed{x = -1}$$