

Name: Solutions

/ 25

There are 25 points possible on this quiz. *You should be able to complete it without using your notes or textbook – this is practice for your exams!* If you needed to look something up, you might want to come talk to me about questions you might have. **Show all work for full credit** and use some words or sentences to help communicate your answers.

1. [11 points] The point $P = (2, 1)$ is a point on the graph of $f(x) = \frac{x}{3-x} - 1$.

a. Find the slope of the secant line passing through P and the point $Q = (0, f(0))$. Show some work.

$$f(0) = \frac{0}{3-0} - 1 = -1, \text{ so slope} = \frac{-1 - 1}{0 - 2} = \frac{-2}{-2} = 1$$

$$\text{so } Q = (0, -1)$$

$$\text{Slope} = \underline{1}$$

b. Find the slope of the secant line passing through P and the point $R = (1, f(1))$. Show some work.

$$f(1) = \frac{1}{3-1} - 1 = \frac{1}{2} - 1 = -\frac{1}{2} \text{ so } R = (1, -\frac{1}{2})$$

$$\text{slope} = \frac{-\frac{1}{2} - 1}{1 - 2} = \frac{-\frac{3}{2}}{-1} = \frac{3}{2}$$

$$\text{Slope} = \underline{\frac{3}{2}}$$

c. The table below lists the slope of the secant line passing through the point P and the point $S = (x, f(x))$ for several values of x . The value m_{sec} is the slope of the secant line.

x	1.9	1.99	1.999	2.001	2.01	2.1
$f(x)$	0.727273	0.970297	0.997003	1.003	1.0303	1.33333
m_{sec}	2.72727	2.97030	2.99700	3.00300	3.03030	3.33333

Use the information in the table to estimate the slope of the tangent line to $f(x)$ at the point $P = (2, 1)$.

$$\text{Tangent line slope} = \underline{3}$$

d. Use the slope from part (c) above to write an equation of the tangent line at point $P = (2, 1)$. You may write the equation of the line in whatever form you choose.

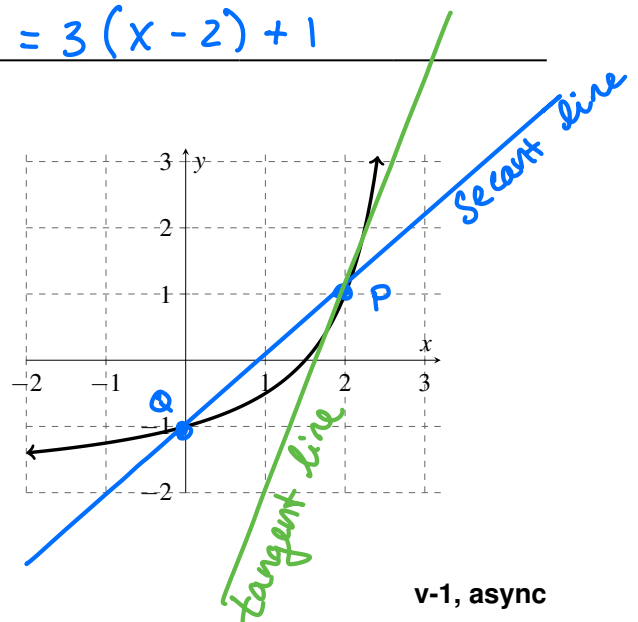
$$\text{Tangent line equation: } \underline{y = 3(x - 2) + 1}$$

e. To the right is a sketch of part of the graph of

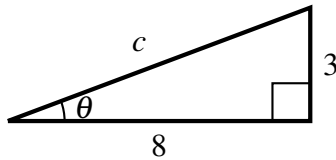
$$f(x) = \frac{x}{3-x} - 1.$$

Sketch and label the **tangent** line to the graph at the point $P = (2, 1)$.

Sketch and label the **secant** line between $P = (2, 1)$ and $Q = (0, f(0))$.



2. [2 points] Use the right triangle below, with side lengths 8, 3 and missing value c , to evaluate the expressions. Give your answers as exact numbers.



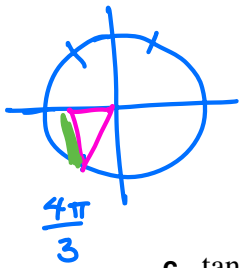
$$c^2 = 8^2 + 3^2 = 64 + 9 = 73 \Rightarrow c = \sqrt{73}$$

$$\text{a. } \tan(\theta) = \frac{\text{opp}}{\text{adj}} = \frac{3}{8}$$

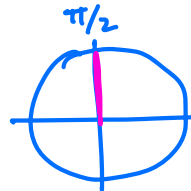
$$\text{b. } \sec(\theta) = \frac{\text{hyp}}{\text{adj}} = \frac{\sqrt{73}}{8}$$

3. [8 points] Evaluate the expressions below. Assume all angles are measured in radians.

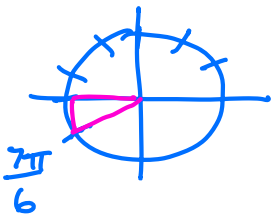
$$\text{a. } \sin(4\pi/3) = -\frac{\sqrt{3}}{2}$$



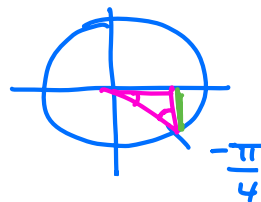
$$\text{b. } \cos(\pi/2) = 0$$



$$\text{c. } \tan(7\pi/6) = \frac{-1/2}{-\sqrt{3}/2} = \frac{1}{\sqrt{3}}$$



$$\text{d. } \sin(-\pi/4) = -\frac{1}{\sqrt{2}}$$



4. [4 points] An athlete is running along a straight path. The position of the athlete is given by $d(t) = \frac{1}{2}t^2 + t$, where t is time measured in seconds and d is distance measured in meters. Find the average velocity of the athlete between $t = 2$ and $t = 5$. Include units with your answer.

$$d(2) = \frac{1}{2}(2)^2 + 2 = \frac{1}{2}(4) + 2 = 4$$

$$d(5) = \frac{1}{2}(5)^2 + 5 = \frac{1}{2}(25) + 5 = \frac{35}{2}$$

$$\begin{array}{r} 23'5 \\ - 8 \\ \hline 27 \end{array}$$

$$\begin{aligned} \text{average velocity} &= \frac{\frac{35}{2} - 4}{5 - 2} = \frac{\frac{27}{2}}{3} = \frac{27}{6} \text{ meters/second} \\ &= \frac{9}{2} \text{ meters/second} \end{aligned}$$