Name: $\qquad$
There are 25 points possible on this quiz. You should be able to complete it without using your notes or textbook - this is practice for your exams! If you needed to look something up, you might want to come talk to me about questions you might have. Show all work for full credit and use some words or sentences to help communicate your answers.

1. [11 points] The point $P=(2,1)$ is a point on the graph of $f(x)=\frac{x}{3-x}-1$.
a. Find the slope of the secant line passing through $P$ and the point $Q=(0, f(0))$. Show some work.

$$
\text { Slope }=
$$

$\qquad$
b. Find the slope of the secant line passing through $P$ and the point $R=(1, f(1))$. Show some work.

$$
\text { Slope }=
$$

$\qquad$
c. The table below lists the slope of the secant line passing through the point $P$ and the point $S=(x, f(x))$ for several values of $x$. The value $m_{\text {sec }}$ is the slope of the secant line.

| $x$ | 1.9 | 1.99 | 1.999 | 2.001 | 2.01 | 2.1 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 0.727273 | 0.970297 | 0.997003 | 1.003 | 1.0303 | 1.33333 |
| $m_{\text {sec }}$ | 2.72727 | 2.97030 | 2.99700 | 3.00300 | 3.03030 | 3.33333 |

Use the information in the table to estimate the slope of the tangent line to $f(x)$ at the point $P=(2,1)$.
Tangent line slope =
$\qquad$
d. Use the slope from part (c) above to write an equation of the tangent line at point $P=(2,1)$. You may write the equation of the line in whatever form you choose.

Tangent line equation: $\qquad$
e.

To the right is a sketch of part of the graph of

$$
f(x)=\frac{x}{3-x}-1
$$

Sketch and label the tangent line to the graph at the point $P=(2,1)$.
Sketch and label the secant line between $P=(2,1)$ and $Q=(0, f(0))$.

2. [2 points] Use the right triangle below, with side lengths 8,3 and missing value $c$, to evaluate the expressions. Give your answers as exact numbers.

a. $\tan (\theta)=$
b. $\sec (\theta)=$
3. [8 points] Evaluate the expressions below. Assume all angles are measured in radians.
a. $\sin (4 \pi / 3)=$
b. $\cos (\pi / 2)=$
c. $\tan (7 \pi / 6)=$
d. $\sin (-\pi / 4)=$
4. [4 points] An athlete is running along a straight path. The position of the athlete is given by $d(t)=\frac{1}{2} t^{2}+t$, where $t$ is time measured in seconds and $d$ is distance measured in meters. Find the average velocity of the athlete between $t=2$ and $t=5$. Include units with your answer.

