September 22, 2023

Math 251: Quiz 4

There are 25 points possible on this quiz. You should be able to complete it without using your notes or textbook - this is practice for your exams! If you needed to look something up, you should to me about questions you might have. Show all work for full credit and use some words or sentences to help communicate your answers. Do not use a calculator.

1. [8 points] Use the limit definition of the derivative to find the derivative of $g(x) = x + \frac{3}{x}$. No credit will be awarded a solution that does not use the definition below. Show all your work clearly, step by step, using correct notation.

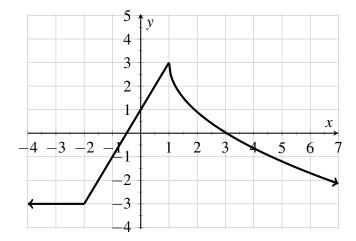
$$g'(x) := \lim_{h \to 0} \frac{g(x+h) - g(x)}{h}$$

- 2. [6 points] A ball is thrown upwards into the air. Its height, in feet, after t seconds is given by the function $s(t) = 40t - 16t^2$
 - **a**. Find the average velocity of the ball over the time interval from t = 1 to t = 2. Include units with your answer.

b. Find the instantaneous velocity of the ball when t = 2. Include units with your answer.

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3. [5 points] The graph of f(x) is below. On the same set of axes, make a rough sketch of the graph of f'(x). If they exist, indicate any asymptotes with dashed lines. Use open circles to show points where the derivative is not defined, if any. Make sure you are writing darkly enough that I can see your graph clearly! (Double-check your scan before you submit.)



4. [6 points] Use the derivative rules to find the derivative for each function below. **Do not simplify your answer.**

a.
$$f(x) = (\sin x)(3x^2 - 5x + 6)$$

b.
$$g(x) = 4x^{1/5} + \frac{9}{x^3} + \sqrt{3} + 10x$$