Name: $\qquad$
There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [4 points] A population of voles is taking over a garden. The table below indicates the size of the population measured at the middle of each week during a summer.

| $t$ (weeks) | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $n$ (voles) | 7 | 15 | 31 | 63 | 73 | 82 |

a. Find the average rate of change of the population over the entire measurement period.
b. Find the average rate of change of the population from week 3 to week 5.
2. [9 points] Use the graph of the function of $f(x)$ to answer the following questions.

a. $\lim _{x \rightarrow 0^{+}} f(x)=$ $\qquad$
b. $\lim _{x \rightarrow 0^{-}} f(x)=$ $\qquad$
c. $\lim _{x \rightarrow 0} f(x)=$ $\qquad$
d. $f(0)=$ $\qquad$
e. $f(5)=$ $\qquad$
f. $f(-6)=$ $\qquad$
g. $\lim _{x \rightarrow-4^{+}} f(x)=$ $\qquad$
h. $\lim _{x \rightarrow 5} f(x)=$ $\qquad$
i. $\lim _{x \rightarrow-6} f(x)=$ $\qquad$
3. [6 points] Compute the following limits. For each limit, justify your answer with a sentence or two.
a. $\lim _{x \rightarrow 8^{+}} \frac{2+x}{(x-8)^{2}}=\square$
b. $\lim _{x \rightarrow \pi^{+}} \frac{\sqrt{2}}{\sin (x)}=\square$
4. [6 points] On the axes below, sketch the graph of the function

$$
f(x)= \begin{cases}2-x & x<1 \\ 3 & x=1 \\ \frac{1}{1-x} & x>1\end{cases}
$$

Then compute, with brief justification, the requested values in the table.


| Value | Justification |
| :---: | :---: |
| $f(1)=$ |  |
| $\lim _{x \rightarrow 1^{-}} f(x)=$ |  |
|  |  |
| $\lim _{x \rightarrow 1} f(x)=$ |  |
|  |  |

