Name: $\qquad$
There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [4 points] The temperature on a Fairbanks January morning is rapidly rising. The table below indicates the temperature in degrees Fahrenheit measured once an hour starting at some initial time $t=0$ hours.

| $t$ (hours) | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T\left({ }^{\circ} \mathrm{F}\right)$ | 2 | 5 | 12 | 18 | 23 | 27 |

a. Find the average rate of change of the temperature over the entire measurement period.
b. Find the average rate of change of the temperature from hour 2 to hour 4.
2. [9 points] Use the graph of the function of $f(x)$ to answer the following questions.

a. $\lim _{x \rightarrow 5^{+}} f(x)=$
b. $\lim _{x \rightarrow 5^{-}} f(x)=$ $\qquad$
c. $\lim _{x \rightarrow 5} f(x)=$ $\qquad$
d. $f(5)=$ $\qquad$
e. $f(0)=$ $\qquad$
f. $f(-6)=$ $\qquad$
g. $\lim _{x \rightarrow-4^{+}} f(x)=$ $\qquad$
h. $\lim _{x \rightarrow 0} f(x)=$ $\qquad$
i. $\lim _{x \rightarrow-6} f(x)=$ $\qquad$
3. [6 points] Compute the following limits. For each limit, justify your answer with a sentence or two.
a. $\lim _{x \rightarrow 2 \pi^{-}} \frac{x+3}{\sin (x)}=\square$
b. $\lim _{x \rightarrow 2^{+}} \frac{\sqrt{5}}{(x-2)^{4}}=\square$
4. [6 points] On the axes below, sketch the graph of the function

$$
f(x)= \begin{cases}x+2 & x<-1 \\ -2 & x=-1 \\ \frac{1}{x+1} & x>-1\end{cases}
$$

Then compute, with brief justification, the requested values in the table.


| Value | Justification |
| :---: | :---: |
| $f(-1)=$ |  |
| $\lim _{x \rightarrow-1} f(x)=$ |  |
| $\lim _{x \rightarrow-1^{-}} f(x)=$ |  |

