

Name: \_\_\_\_\_

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There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

**1. [4 points]**

a. Why is the following not a true statement?  $\frac{x^2 - 6x}{x} = x - 6$

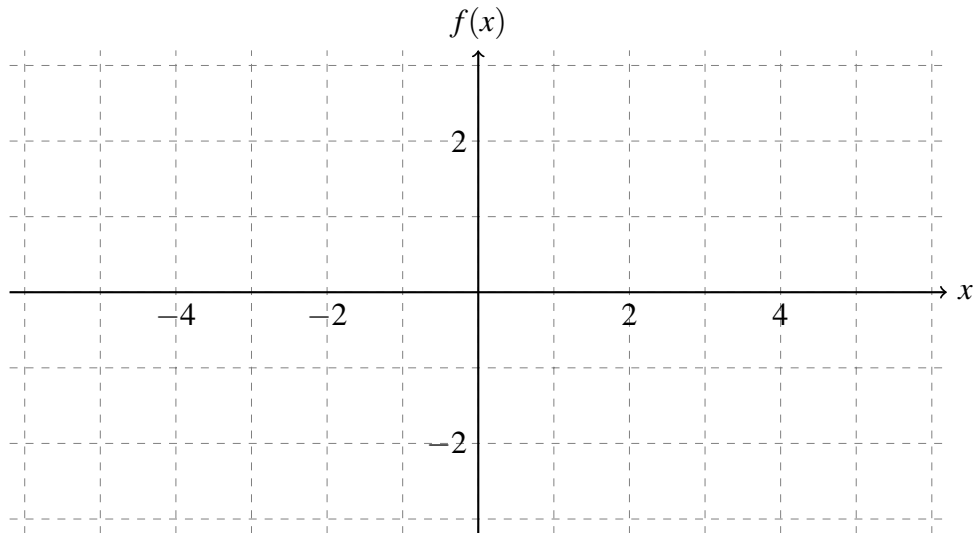
b. Nevertheless, explain why the following equation is correct.  $\lim_{x \rightarrow 0} \frac{x^2 - 6x}{x} = \lim_{x \rightarrow 0} x - 6$

2. [4 points] Compute  $\lim_{x \rightarrow 5} \frac{\frac{1}{5} - \frac{1}{x}}{5 - x}$ .

3. [4 points] Compute  $\lim_{h \rightarrow 0} \frac{(2+h)^2 - 4}{h}$

4. [6 points] Consider the function  $f(x) = \begin{cases} \frac{3}{1-x} & x \leq 0 \\ 3 \sin(x) & x > 0. \end{cases}$

a. In the diagram below, graph  $f(x)$ .



b. Explain why  $f(x)$  isn't continuous at  $x = 0$ .

5. [4 points] Use the Intermediate Value Theorem to justify the claim that there exists a number  $x$  satisfying  $2^x - x - 4 = 0$ .