

Name: \_\_\_\_\_

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There are 30 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [15 points] Compute the derivatives of the following functions.

a.  $f(x) = 2 + \sqrt{x} - e^x$

$$f'(x) = 0 + \frac{1}{2}x^{-1/2} - e^x = \frac{1}{2}x^{-1/2} - e^x$$

b.  $f(r) = \frac{3}{r^3} = 3r^{-3}$

$$f'(r) = -9r^{-4} = -\frac{9}{r^4}$$

c.  $f(x) = \frac{\sqrt[3]{x} + 5}{x}$ . Hint: Don't bother with the quotient rule.

$$\begin{aligned} f(x) &= x^{\frac{1}{3}-1} + 5x^{-1} & f'(x) &= \frac{-2}{3}x^{-5/3} - 5x^{-2} \\ &= x^{-2/3} + 5x^{-1} \end{aligned}$$

d.  $f(x) = x^{-1/2}e^x$

$$f'(x) = -\frac{1}{2}x^{-3/2}e^x + x^{-1/2}e^x$$

e.  $f(x) = \frac{x^2+1}{x^2-1}$

$$\begin{aligned} f'(x) &= \frac{2x(x^2-1) - 2x(x^2+1)}{(x^2-1)^2} \\ &= \frac{-4x}{(x^2-1)^2} \end{aligned}$$

2. [5 points] A population of moose is declining. The population at time  $t$  is

$$P(t) = \frac{1000}{1+t}$$

where  $P$  is the number of moose and where  $t$  is measured in years.

Compute the rate of change of the moose population, with units, at time  $t = 4$  years.

$$P'(t) = \frac{0 \cdot (1+t) - 1000 \cdot 1}{(1+t)^2} = \frac{-1000}{(1+t)^2}$$

$$P'(4) = \frac{-1000}{25} = -40 \text{ moose/year}$$

3. [6 points] A particle is moving along a line, and its position  $x$  as a function of time  $t$  is

$$x(t) = (1-t^2)e^t.$$

- a. Compute the velocity of the particle.

$$\begin{aligned} x'(t) &= -2te^t + (1-t^2)e^t \\ &= (1-2t-t^2)e^t \end{aligned}$$

- b. Compute the acceleration of the particle.

$$\begin{aligned} x''(t) &= (-2-2t)e^t + (1-2t-t^2)e^t \\ &= -(1+4t+t^2)e^t \end{aligned}$$

4. [4 points] Find the formula for the tangent line to the curve  $y = x - x^3$  at  $x = 2$ .

$$\begin{array}{l|l} \textcircled{A} x=2 & y = 2 - 2^3 = -6 \\ & y' = 1 - 3x^2 \\ \textcircled{B} x=2 & y' = 1 - 3 \cdot 4 \\ & = -11 \end{array} \left. \begin{array}{l} \text{point-slope form} \\ y + 6 = -11(x - 2) \\ y = -6 - 11(x - 2) \end{array} \right\}$$