_____/ 20

Name: _____

There are 20 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [12 points] Compute the derivatives of the following functions. Simplify your answers.

Math 251: Quiz 5

2. [4 points] The length of a day in a certain city is given by

$$L(t) = 12 + 6\sin\left(2\pi\frac{t - 80}{365}\right).$$

where *L* is measured in hours and *t* is measured in days, with t = 0 representing January 1.

a. Compute L'(t).

$$\begin{bmatrix} 2\pi (t) = 6 \cos \left(2\pi \left(\frac{t-80}{365}\right)\right) \cdot \frac{2\pi}{365} \\ = \frac{12\pi}{365} \cos \left(2\pi \left(\frac{t-80}{365}\right)\right) \cdot \frac{2\pi}{365} \end{bmatrix}$$

b. Suppose you have computed $L'(245) \approx -0.1$. Interpret what this means in precise language that your parents could nevertheless understand. Your answer must include units for full credit.

3. [4 points] Determine all times *t* such that the graph of $y = 2x - \sin(2x)$ has a horizontal tangent.

$$\frac{dy}{dx} = 2 - 2\cos(2x) ; we want \frac{dy}{dx} = 2$$

$$2 - 2\cos(2x) = 0$$

$$\cos(2x) = 1$$

$$2x = 2\pi k$$

$$x = \pi k, k \text{ any integer}$$