Name: $\qquad$
$\qquad$ / 30

There are 30 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [5 points] Sketch a function on $[-5,5]$ that has an absolute maximum value of 3 at $x=4$, an absolute minimum value of -2 at $x=-4$, and a local maximum at $x=1$. You should appropriately label notable values on the $x$ - and $y$-axes for full credit.

2. [5 points] Find all critical numbers (a.k.a. critical points) of the function $f(x)=x(x-1)^{1 / 3}$. Be careful!
3. [10 points] Find the maximum and minimum values of the function $f(x)=1 / x-1 / x^{2}$ on the interval $[1,10]$.
4. [5 points] Suppose $f$ is continuous on $[-2,2]$ and has a derivative at each point in $(-2,2)$. Suppose $f(-2)=6$ and $f(2)=-4$. What does the Mean Value Theorem let you conclude?
5. [5 points] Draw a diagram that illustrates the Mean Value Theorem in the context of the previous problem. Your illustration should include a tangent line somewhere.

