## Name: \_\_\_\_\_

## Circle one: Rhodes (F01) | Bueler (F02)

25 points possible. No aids (book, calculator, etc.) are permitted. Show all work and use proper notation for full credit.

LITIONS

**1.** [6 points] A particle is moving with the given acceleration a(t) and other data. Find the position s(t) of the particle.



2. [6 points] The graph of f is shown. Evaluate each integral by interpreting it in terms of areas.



a. 
$$\int_{-2}^{0} f(x) dx = 3 \cdot 2 = 6$$
  
b. 
$$\int_{4}^{0} f(x) dx = -\int_{0}^{4} f(x) dx = -\left(\frac{1}{2} \cdot 3 \cdot 1 - \frac{1}{2} \cdot 3 \cdot 3\right) = 3$$
  
c. 
$$\int_{-2}^{4} f(x) dx = \int_{-2}^{0} f(x) dx + \int_{0}^{4} f(x) dx = 6 - 3 = 3$$

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**UAF Calculus I** 

## Math 251: Quiz 9

**3.** [8 points] Consider the graph of  $f(x) = \frac{1}{1+x}$  below.



- a. In the figure above, sketch four rectangles corresponding to the n = 4 Riemann sum on the interval  $1 \le x \le 3$ . Use right endpoints.  $f(\frac{3}{2}) = \frac{2}{5}$ ,  $f(2) = \frac{1}{5}$ ,  $f(\frac{5}{2}) = \frac{2}{5}$ ,  $f(\frac{5}{2}) = \frac{2$
- **b**. Compute the numerical value of the Riemann sum illustrated in part **a**. Express your answer as a single fraction.

$$\begin{cases} q = f(\frac{3}{2}) \cdot \frac{1}{2} + f(2) \cdot \frac{1}{2} + f(\frac{5}{2}) \cdot \frac{1}{2} + f(3) \cdot \frac{1}{2} \\ = \frac{1}{2} \left(\frac{2}{5} + \frac{1}{3} + \frac{2}{7} + \frac{1}{4}\right) = \frac{1}{2} \left(\frac{168 + 140 + 120 + 105}{420}\right) \\ = \frac{1}{2} - \frac{533}{420} = \left(\frac{533}{840}\right)$$
Is your numerical value in part h an overestimate or an underestimate of  $\int_{1}^{3} \frac{1}{4} dx^{2}$ 

**c**. Is your numerical value in part **b** an overestimate or an underestimate of  $\int_1^{\infty} \frac{1}{1+x} dx$ ?

**4.** [5 points] Use the Midpoint Rule with n = 2 subintervals to approximate the integral. Express your answer as a single fraction.

$$\int_{0}^{4} x 2^{-x} dx \approx Z \cdot f(1) + 2 \cdot f(3)$$
  
=  $2 \cdot (1 \cdot 2^{-1}) + 2 \cdot (3 \cdot 2^{-3})$   
=  $\frac{2}{2} + \frac{2 \cdot 3}{2^{3}} = \begin{pmatrix} 7 \\ -4 \end{pmatrix}$ 

$$f(x)=x2^{-x}$$