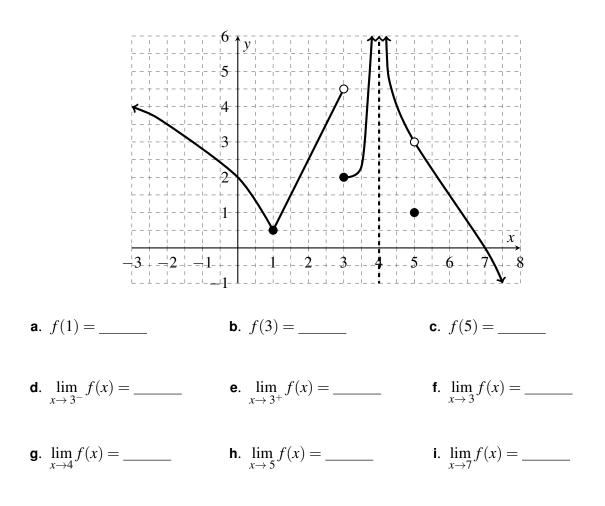
## Name: \_

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There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [11 points] Use the graph of the function H(x) (drawn below) to answer the questions. Assume H(x) has a vertical asymptote at x = 4. For each problem below, give the most complete answer; if the limit is infinite, indicate that with  $\infty$  or  $-\infty$ . If a value does not exist, write DNE.



j. List all *x*-values for which the function H(x) fails to be continuous.

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**2.** [10 points] Evaluate the following limits. Give the most complete answer; if the limit is infinite, indicate that with  $\infty$  or  $-\infty$ . If a value does not exist, write DNE. You must show work to receive full credit.

**a.** 
$$\lim_{x \to 4} \frac{2x^2 - 8x}{x^2 - x - 12}$$

**b.** 
$$\lim_{x \to 1} \frac{\sqrt{3+x}-2}{x-1}$$

$$c. \lim_{x \to -2^+} \frac{5x}{x+2}$$

**d**. Given 
$$\lim_{x \to 10} f(x) = 5$$
 and  $\lim_{x \to 10} g(x) = -3$ , evaluate  $\lim_{x \to 10} 2\left(\frac{x+1}{f(x)+g(x)}\right)$ .

**3.** [4 points] Use the Intermediate Value Theorem to show that the polynomial  $p(x) = x^3 - x + 2$  must reach a *y*-value of 5 for some *x*-value on the interval [1,2].