Math 251: Quiz 10

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Name: ____

There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [5 points] Find the derivatives.

a.
$$G(x) = \int_0^x \sqrt{1 + 2t^2} \, dt$$

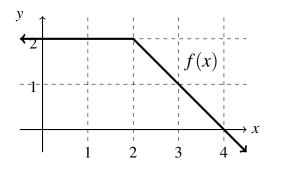
b.
$$H(x) = \int_{1}^{x^{3}} 8\sin\left(\frac{1}{t}\right) dt$$

- **2.** [6 points] The velocity of a particle moving along a straight line is given by $v(t) = t^2 1$ where $0 \le t \le 2$ is measured in seconds and v is measured in meters per second.
 - **a**. Find the **displacement** of the particle between t = 0 and t = 2.

b. Find the **distance traveled** of the particle between t = 0 and t = 2.

c. Does the problem contain sufficient information to determine the position of the particle at time t = 2? If so, determine the position. If not, explain why not.

3. [4 points] Use the graph of f(x) (below) to answer questions about $A(x) = \int_0^x f(t) dt$.



- **a**. A(0) =
- **b**. A(4) =
- **c**. At x = 3, is A(x) increasing, decreasing, or neither?
- 4. [12 points] Evaluate the definite integrals below.

a.
$$\int_{1}^{3} (2-6x^2) dx$$

b.
$$\int_0^1 \sin(5x) \, dx$$

c.
$$\int_0^2 \frac{x^2}{\sqrt{1+x^3}} dx$$