Name: _____

There are 25 points possible on this quiz. No aids (book, calculator, etc.) are permitted. Show all work for full credit.

1. [2 points] Use the Fundamental Theorem of Calculus to evaluate the following derivative:

$$\frac{d}{dx}\left(\int_{x}^{7}\sqrt{|t+8|}\,dt\right)$$

2. [12 points] Evaluate the following indefinite integrals. Show your work and state whenever you use a substitution.

a.
$$\int x^2 (x^3 - 2)^2 dx$$

b.
$$\int \sin x \cos x \, dx$$

$$c. \quad \int \frac{\ln x + 3}{x} \, dx$$

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3. [5 points] Find the area under the curve $f(x) = x^2 + 2x + e^x$ from x = 0 to x = 3. Use a definite integral, show all your work, and simplify your final answer.

4. [6 points] A ball is thrown upward from an initial height of 5 feet at an initial speed of 40 feet per second. Its upward velocity at *t* seconds is given by the equation v(t) = -32t + 40 feet per second.

a. Evaluate
$$\int_0^2 v(t) dt$$
.

b. Explain what the quantity $\int_0^2 v(t) dt$ represents. Give units.

c. Explain how would this answer change if the ball had been thrown from an initial height of 10 feet?