Name: $\qquad$

30 minutes maximum. 25 possible points. No aids (book, calculator, etc.) are permitted Show all work and use proper notation for full credit. Answers should be in reasonably-simplified form.

For each problem below, you are strongly encouraged to sketch the region and draw a sample slice.

1. [8 points] Find the area of the region enclosed by $y=5-x^{2}$ and $y=3-x$.
2. [8 points] Find the volume of the solid obtained by rotating region determined by $y=e^{-x}, y=0$, $x=-1$, and $x=1$ about the $x$-axis.
3. [9 points points] Let $R$ be the region bounded by $y=2 x^{2}$ and $y=x^{3}$, graphed below. Set up an integral to find the volume of the solid obtained if:

a. $R$ rotated about the $x$-axis.
b. $R$ rotated about the $y$-axis.
c. $R$ is the base of a solid with cross-sections perpendicular to the base and parallel to the $y$-axis are squares.
