

Thirty minutes maximum. No aids (book, notes, calculator, phone, etc.) are permitted. Show all work and use proper notation for full credit. Answers should be in reasonably simplified form.

1. Let $f(x) = \sqrt[3]{x}$.

(a) (8 points.) Find the first order and second order Taylor polynomials for $f(x)$ centered at $a = 8$.

(b) (8 points.) Use the first order Taylor polynomial to estimate $\sqrt[3]{7}$.

2. (8 points.) Find the Taylor series for $g(x) = \ln(x)$ centered at $a = 1$ (Wait, haven't we seen this before?).

3. (8 points.) Find the radius and interval of convergence for the Taylor series you found in problem 2 above.

RADIUS OF CONVERGENCE: _____ INTERVAL OF CONVERGENCE: _____

BONUS (5 points) What is the 32nd derivative of $f(x) = e^{x^2}$ at $x = 0$. I.E., find $f^{(32)}(0)$. (Hey, this looks familiar too!).