1. Find the Taylor series for the function $f(x)=\sin (x)$ centered at $a=\pi$.
2. Use the integral test to determine whether $\sum_{n=1}^{\infty} n e^{-n^{2}}$ converges or diverges.
3. Determine whether the series $\sum_{n=1}^{\infty}(-1)^{n} \frac{\sqrt{n}}{2 n+3}$ is absolutely convergent, conditionally convergent or divergent. You must clearly explain your reasoning.
4. Find the radius of convergence and the interval of convergence of the following series.
(a) $\sum_{n=1}^{\infty} n!(2 x-1)^{n}$
(b) $\sum_{n=1}^{\infty} \frac{(x-a)^{n}}{n b^{n}}$, where $a$ and $b$ are positive constants.
5. Consider $x=t^{2}+1, y=e^{2 t}-1$.
(a) Find $\frac{d y}{d x}$.
(b) Determine the location of any horizontal tangents. If none exist, explain why.
(c) Find $\frac{d^{2} y}{d x^{2}}$.
(d) Determine the concavity of the graph when $t=1$.
6. Consider the curve $r=1+2 \cos \theta$.
(a) Sketch the curve $r=1+2 \cos \theta$. Include the coordinates of all $x$ - and $y$-intercepts.

(b) Find the area enclosed by the inner loop.
7. For each problem below, set up an integral(s) to find the quantity.
(a) Find the mass of a wire that is 2 meters long (starting at $x=0$ ) and has density $\rho(x)=3 x+1$ grams per meter.
(b) Let $\mathcal{R}$ be the region bounded by $y=e^{x}$ and $y=0,0 \leq x \leq 2$. If the density of the region is given by $\rho=5$, find the center of mass of $R$ (or, equivalently, find the centroid of $R$.)
(c) Recall that in the metric system force, $F$, is often measured in newtons ( $N$ ) and work, $W$, is often measured in joules $(j)$ or newton-meters $(N \cdot m)$. Suppose a spring has a natural length of 15 cm and exerts a force of 8 N when stretched to a length of 20 cm . How much work is done stretching the spring from 15 cm to 25 cm ?
