

### SECTION 3.3: TRIGONOMETRIC SUBSTITUTION (DAY 1)

1. Compare the following three integrals:

(a)  $\int x\sqrt{9-x^2} dx$

(b)  $\int \frac{dx}{\sqrt{9-x^2}}$

(c)  $\int \sqrt{9-x^2} dx$

2. Summary: If  $\sqrt{a^2 - x^2}$  appears in an integrand (**and** other techniques do not work), then

3. Evaluate  $\int \frac{dx}{x^2\sqrt{4-x^2}}$

4. Compare the following integrals:

(a)  $\int x\sqrt{9+x^2} dx$

(b)  $\int \frac{dx}{9+x^2}$

(c)  $\int \frac{dx}{\sqrt{9+x^2}}$

(d)  $\int \frac{dx}{\sqrt{x^2-9}} dx$

5. Summary:

- If  $\sqrt{a^2 + x^2}$  appears in an integrand (**and** other techniques do not work), then
- If  $\sqrt{x^2 - a^2}$  appears in an integrand (**and** other techniques do not work), then

6. Evaluate

(a)  $\int \frac{\sqrt{4+x^2}}{x} dx$

(b)  $\int \frac{dx}{(x^2-9)^{3/2}}$